

Risk Aversion and the Labor Margin in Dynamic Equilibrium Models

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Coefficient of Relative Risk Aversion

Suppose a household has preferences:

$$E_0 \sum_{t=0}^{\infty} \beta^t u(c_t, l_t),$$

$$u(c_t, l_t) = \frac{c_t^{1-\gamma}}{1-\gamma} - \eta l_t$$

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Answer: 0

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What is the household's coefficient of relative risk aversion?

Answer: $\frac{1}{\frac{1}{\gamma} + \frac{1}{\chi}}$

Outline of Presentation

- Define risk aversion rigorously in dynamic equilibrium models
- Derive closed-form expressions
- Show the labor margin has dramatic effects on risk aversion

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See the paper for:

- Epstein-Zin preferences
- internal, external habits
- asset pricing details
- numerical computations

A Household

Household preferences:

$$E_t \sum_{\tau=t}^{\infty} \beta^{\tau-t} u(c_{\tau}, l_{\tau}),$$

Flow budget constraint:

$$a_{\tau+1} = (1 + r_{\tau})a_{\tau} + w_{\tau}l_{\tau} + d_{\tau} - c_{\tau},$$

No-Ponzi condition:

$$\lim_{T \rightarrow \infty} \prod_{\tau=t}^T (1 + r_{\tau+1})^{-1} a_{T+1} \geq 0,$$

$\{w_{\tau}, r_{\tau}, d_{\tau}\}$ are exogenous processes, governed by θ_{τ}

The Value Function

State variables of the household's problem are $(\mathbf{a}_t; \theta_t)$.

Let:

$$c_t^* \equiv c^*(\mathbf{a}_t; \theta_t),$$

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Value function, Bellman equation:

$$V(a_t; \theta_t) = u(c_t^*, l_t^*) + \beta E_t V(a_{t+1}^*; \theta_{t+1}),$$

where:

$$a_{t+1}^* \equiv (1 + r_t)a_t + w_t l_t^* + d_t - c_t^*.$$

Technical Conditions

Assumption 1. *The function $u(c_t, l_t)$ is increasing in its first argument, decreasing in its second, twice-differentiable, and strictly concave.*

Assumption 2. *The value function $V : X \rightarrow \mathbb{R}$ for the household's optimization problem exists and satisfies the Bellman equation*

$$V(a_t; \theta_t) = \max_{(c_t, l_t) \in \Gamma(a_t; \theta_t)} u(c_t, l_t) + \beta E_t V(a_{t+1}; \theta_{t+1}).$$

Assumption 3. *For any $(a_t; \theta_t) \in X$, the household's optimal choice (c_t^*, l_t^*) lies in the interior of $\Gamma(a_t; \theta_t)$.*

Assumption 4. *The value function $V(\cdot; \cdot)$ is twice-differentiable. (It then follows that c^*, l^* are differentiable.)*

Assumptions about the Economic Environment

Assumption 5. *The household is atomistic.*

Assumption 6. *The household is representative.*

Assumption 7. *The model has a nonstochastic steady state, $x_t = x_{t+k}$ for $k = 1, 2, \dots$, and $x \in \{c, l, a, w, r, d, \theta\}$.*

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Assumption 7'. *The model has a balanced growth path that can be renormalized to a nonstochastic steady state after a suitable change of variables.*

Arrow-Pratt in a Static One-Good Model (Review)

Compare:

$$E u(c + \sigma \varepsilon) \quad \text{vs.} \quad u(c - \mu)$$

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$$E u(c + \sigma \varepsilon) \approx u(c) + u'(c)\sigma E[\varepsilon] + \frac{1}{2}u''(c)\sigma^2 E[\varepsilon^2],$$

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Coefficient of absolute risk aversion is defined to be:

$$\lim_{\sigma \rightarrow 0} 2\mu(\sigma)/\sigma^2 = \frac{-u''(c)}{u'(c)}.$$

Intro
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Framework
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Absolute Risk Aversion
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Relative Risk Aversion
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Examples
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Conclusions
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$$a_{t+1} = (1 + r_t)a_t + w_t l_t + d_t - c_t + \sigma \varepsilon_{t+1}, \quad (*)$$

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Note also (*) is equivalent to gambles over income:

$$a_{t+1} = (1 + r_t)a_t + w_t l_t + (d_t + \sigma \varepsilon_{t+1}) - c_t,$$

or asset returns:

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Note connection to asset pricing.

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Welfare loss from μ :

$$V_1(a_t; \theta_t) \frac{\mu}{(1 + r_t)}$$

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Loss from σ :

$$\beta E_t V_{11}(a_{t+1}^*; \theta_{t+1}) \frac{\sigma^2}{2}.$$

Coefficient of Absolute Risk Aversion

Proposition 1. *The household's coefficient of absolute risk aversion at $(a_t; \theta_t)$ is given by:*

$$\frac{-E_t V_{11}(a_{t+1}^*; \theta_{t+1})}{E_t V_1(a_{t+1}^*; \theta_{t+1})}.$$

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Evaluated at the nonstochastic steady state, this simplifies to:

$$\frac{-V_{11}(a; \theta)}{V_1(a; \theta)}.$$

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Solve for V_1 and V_{11}

Benveniste-Scheinkman:

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Differentiate (*) to get:

$$V_{11}(a_t; \theta_t) = (1 + r_t) \left[u_{11}(c_t^*, l_t^*) \frac{\partial c_t^*}{\partial a_t} + u_{12}(c_t^*, l_t^*) \frac{\partial l_t^*}{\partial a_t} \right].$$

Solve for $\partial l_t^* / \partial a_t$ and $\partial c_t^* / \partial a_t$

Household intratemporal optimality: $-u_2(c_t^*, l_t^*) = w_t u_1(c_t^*, l_t^*)$.

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Use Euler equation and budget constraint to derive:

$$\frac{\partial c_t^*}{\partial a_t} = \frac{r}{1 + w\lambda}.$$

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Proposition 2. *The household's coefficient of absolute risk aversion in Proposition 1, evaluated at steady state, satisfies:*

$$\frac{-V_{11}(a; \theta)}{V_1(a; \theta)} = \frac{-u_{11} + \lambda u_{12}}{u_1} \frac{r}{1 + w\lambda}.$$

Relative Risk Aversion

Consider Arrow-Pratt gamble of general size A_t :

$$a_{t+1} = (1 + r_t)a_t + w_t l_t + d_t - c_t + A_t \sigma \varepsilon_{t+1},$$

vs.

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Risk aversion coefficient for this gamble:

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A natural benchmark for A_t is household wealth at time t .

Household Wealth

In DSGE framework, household wealth has more than one component:

- present value of labor income, $w_t l_t$
- present value of net transfers, d_t
- present value of leisure, $w_t(\bar{l} - l_t)$?

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Leisure, in particular, can be hard to define, e.g.,

$$u(c_t, l_t) = \frac{c_t^{1-\gamma}}{1-\gamma} - \eta \frac{l_t^{1+\chi}}{1+\chi}$$

and \bar{l} is arbitrary.

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and \bar{l} is arbitrary.

Different definitions of household wealth lead to different definitions of relative risk aversion.

Two Coefficients of Relative Risk Aversion

Definition 1. The *consumption-based* coefficient of relative risk aversion is given by (*), with $A_t \equiv (1 + r_t)^{-1} E_t \sum_{\tau=t}^{\infty} m_{t,\tau} c_{\tau}^*$.

In steady state:

$$\frac{-A V_{11}(a; \theta)}{V_1(a; \theta)} = \frac{-u_{11} + \lambda u_{12}}{u_1} \frac{c}{1 + w\lambda}.$$

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$$\tilde{A}_t \equiv (1 + r_t)^{-1} E_t \sum_{\tau=t}^{\infty} m_{t,\tau} (c_{\tau}^* + w_{\tau}(\bar{l} - l_{\tau}^*)).$$

In steady state:

$$\frac{-\tilde{A} V_{11}(a; \theta)}{V_1(a; \theta)} = \frac{-u_{11} + \lambda u_{12}}{u_1} \frac{c + w(\bar{l} - l)}{1 + w\lambda}.$$

Example 1

Utility kernel:

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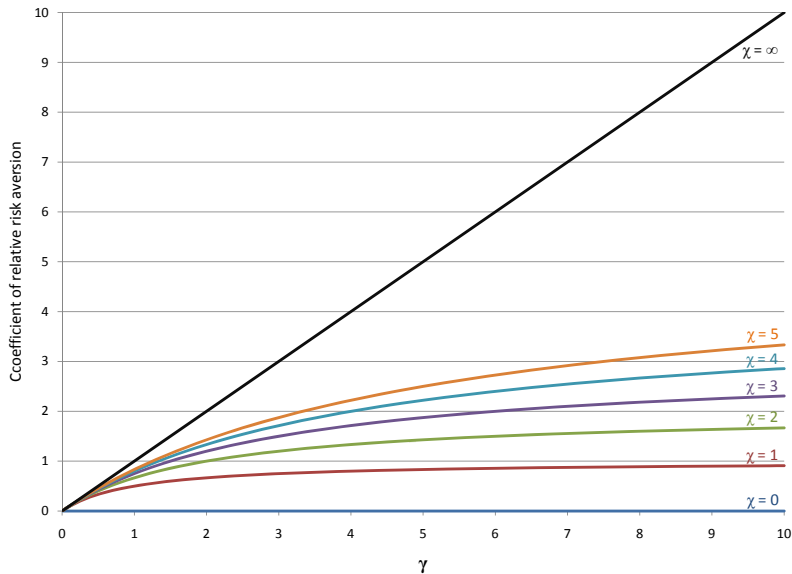
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Example 1



Risk Aversion Away from the Steady State

Utility:

$$u(c_t, l_t) = \frac{c_t^{1-\gamma}}{1-\gamma} - \eta \frac{l_t^{1+\chi}}{1+\chi} \quad \gamma = 2, \chi = 1.5$$

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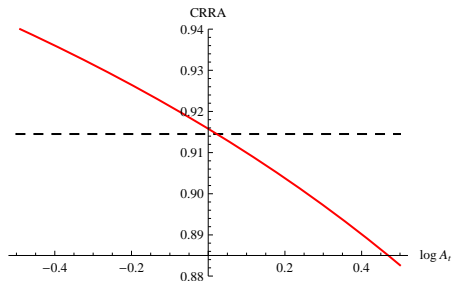
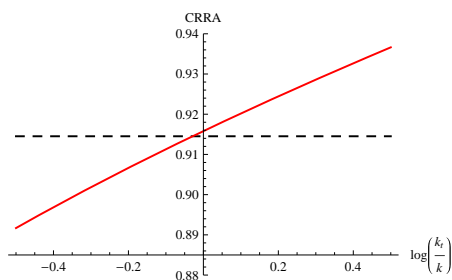
Plus standard RBC model, solved numerically:

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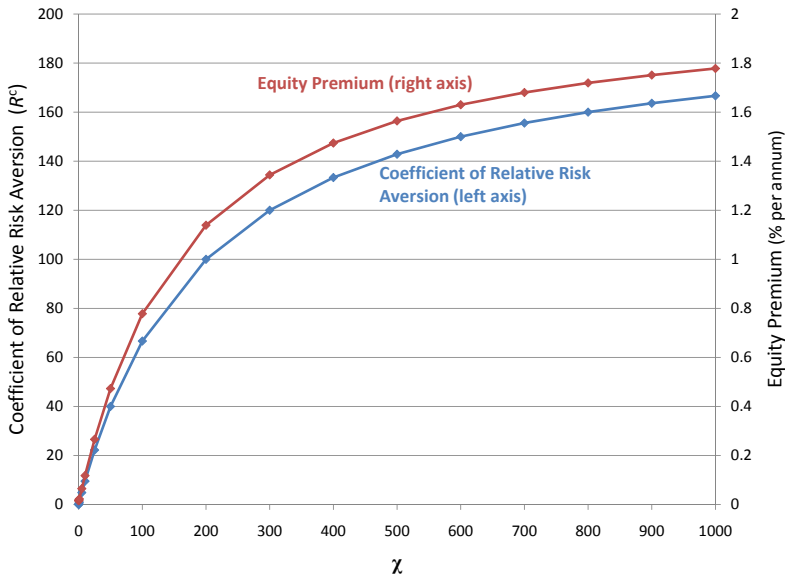
Utility:

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Risk Aversion and the Equity Premium ($\gamma = 200$)



Conclusions

- 1 The labor margin has dramatic effects on risk aversion
- 2 Risk aversion is the right concept for asset pricing, $E_t m_{t+1} p_{t+1}$
- 3 Arrow-Pratt risk neutrality holds for any u with $u_{11}u_{22} - u_{12}^2 = 0$
- 4 Risk aversion and the intertemporal elasticity of substitution are nonreciprocal when there is labor in the model
- 5 Simple, closed-form expressions for risk aversion in DSGE models with:
 - expected utility preferences
 - Epstein-Zin preferences
 - external or internal habits
 - valid away from steady state